The influence of A-cation disorder on the Curie temperature of ferroelectric ATiO₃ perovskites

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The ferroelectric Curie temperature $T_{\rm C}$ in ATiO₃ perovskites is shown to increase linearly with the size variance of the Asite cation mixture [A = (Ba, Sr, Ca)] and this effect accounts for the unusual $T_{\rm C}$ variation in the Ba_{1-x}Ca_xTiO₃ system.

BaTiO₃ is a ferroelectric perovskite widely used in capacitors, thermistors and piezoelectric devices. The Curie temperature above which BaTiO₃ changes from being tetragonal and ferroelectric to cubic and paraelectric is $T_{\rm C} = 403$ K.¹ The ferroelectricity arises from displacements of the Ti atoms towards one of the octahedrally coordinating oxygen atoms along the *c*-axis. A complete solubility exists between BaTiO₃ and SrTiO₃, and $T_{\rm C}$ decreases across the series to a value of 110 K for SrTiO₃.² This trend was ascribed to a cation size effect, in which the smaller Sr ion causes a reduction in the average radius of the A cation site and stabilises the cubic ATiO₃ structure to lower temperatures. By contrast, in the Ba_{1-x}Ca_xTiO₃ system, $T_{\rm C}$ rises from 403 K to a maximum value of 410 K at x = 0.08before dropping to 391 K at the solid solution limit of x = 0.24.³ This variation is not consistent with the above size effect.

It has recently been shown that the electronic and structural phase transition temperatures of several perovskite-type materials vary with the mean size and the size mismatch of the cations on the A-site.^{4,5} Size is parameterised by the mean A-cation radius, $\langle r_A \rangle$, and A-site size mismatch is described by the statistical variance in the distribution of the radii, σ^2 :

$$\sigma^2 = \langle r_{\rm A}^2 \rangle - \langle r_{\rm A} \rangle^2$$

 σ^2 is defined for a mixture of many cations, but in a binary system such as A = (Ba_{1-x}M_x), it reduces to:

$$\sigma^2 = x(1-x)(r_{\rm Ba}-r_{\rm M})^2$$

and hence σ^2 varies quadratically with *x*. At a constant $\langle r_A \rangle$, the temperatures of the ferromagnetic metal to paramagnetic insulator transition in AMnO₃ perovskites (at which colossal magnetoresistances are observed),⁶ and the superconducting critical transitions in A₂CuO₄ and ABa₂CuO₇ decrease linearly with increasing $\sigma^{2.5,7}$ However, the orthorhombic–tetragonal structural transition in the A₂CuO₄ materials shows a strong linear increase with $\sigma^{2.5}$ Here, we present the first systematic study of the influence of A site disorder on the properties of BaTiO₃-based ferroelectric perovskites.

Six (Ba, Sr, Ca)TiO₃ compositions (Table 1) were chosen to give a constant $\langle r_A \rangle = 1.454$ Å but variable σ^2 . $\langle r_A \rangle$ and σ^2 were calculated using standard values of nine-coordinate ionic radii.⁸ 10 g samples were prepared by mixing appropriate quantities of BaCO₃, SrCO₃, CaCO₃ and TiO₂ (all 99.99+% pure) which were ground in an agate mortar and pestle with acetone for 15 min, fired in Pt foil boats at 1000 °C for 12 h, then reground for 15 min before refiring at 1200 and 1350 °C. Regrinding and refiring at 1350 °C for 12 h was repeated six times. The powders were milled in a planetary ball mill for 5 min rather than a mortar and pestle for the final three cycles. This lengthy preparative procedure was necessary as it is known to be difficult to homogenise low levels of alkaline earth dopants in BaTiO₃ powders.⁹

Table 1 Starting and EPMA analysed compositions for six $(Ba_{0.90+0.45x}Sr_{0.1-x}Ca_{0.55x})TiO_3$ samples and their A site cation size variances

Starting composition	Analysed formula ^a	$\sigma^2/\text{\AA}^2$
$\begin{array}{l} Ba_{0.900}Sr_{0.100}TiO_{3}\\ Ba_{0.909}Sr_{0.080}Ca_{0.011}TiO_{3}\\ Ba_{0.918}Sr_{0.060}Ca_{0.022}TiO_{3}\\ Ba_{0.925}Sr_{0.040}Ca_{0.033}TiO_{3}\\ Ba_{0.925}Sr_{0.020}Ca_{0.044}TiO_{3}\\ Ba_{0.945}Ca_{0.055}TiO_{3}\\ \end{array}$	$\begin{array}{l} Ba_{0.91(3)}Sr_{0.09(3)}Ti_{1.0(4)}O_3\\ Ba_{0.90(2)}Sr_{0.09(2)}Ca_{0.01(2)}Ti_{1.02(2)}O_3\\ Ba_{0.92(1)}Sr_{0.06(1)}Ca_{0.02(1)}Ti_{1.02(2)}O_3\\ Ba_{0.93(1)}Sr_{0.04(1)}Ca_{0.03(1)}Ti_{1.02(2)}O_3\\ Ba_{0.94(1)}Sr_{0.02(1)}Ca_{0.04(1)}Ti_{1.02(2)}O_3\\ Ba_{0.95(1)}Ca_{0.05(1)}Ti_{1.03(1)}O_3\\ \text{by normalising to } Ba+Sr+Ca=1. \end{array}$	0.0023 0.0028 0.0032 0.0037 0.0041 0.0047

The samples were characterised by electron probe microanalysis (EPMA), using a Cameca SX51 microprobe, and powder X-ray diffraction on a Stoe STADI/P diffractometer. The L_{α} line of Ba and the K α line of Sr, Ti and Ca were used for the cation analysis, by employing calibration standards of BaTiSi₃O₉, SrTiO₃ and CaSiO₃ and the oxygen contents were calculated by difference. The EPMA showed the samples to be homogeneous with compositions consistent with the starting formulae (Table 1). The room temperature diffraction patterns were obtained with monochromated Cu-K α_1 radiation and were all fully indexed in the tetragonal space group *P4mm*. A linear variation of lattice parameters with σ^2 is observed (Fig. 1), however, the cell volumes for all samples (64.10 ± 0.09 Å³) were the same within error and showed no significant variation with σ^2 .

The ferroelectric Curie temperatures, $T_{\rm C}$, were found from permittivity and calorimetric measurements. Pellets for the permittivity experiments were cold pressed and fired overnight at 1350 °C in air. Impedance was measured between 25 and 180 °C over the frequency range 10–10⁷ Hz with an applied voltage of 100 mV using a 4192 Hewlett Packard impedance analyser. Data obtained at fixed frequency of 1 kHz showed sharp permittivity *vs*. temperature profiles for all the samples, with no apparent broadening of the ferroelectric transition, $T_{\rm C}$ values were extracted from the permittivity maximum obtained



Fig. 1 Variation in the tetragonal lattice parameters of the ATiO₃ samples with σ^2 at 300 K.



Fig. 2 Variation in $T_{\rm C}$ with σ^2 . Open and filled circles correspond to data obtained from permittivity and DSC measurements, respectively.

on a heating cycle. Such values are dependent on the thermal history of the sample, as BaTiO₃-based materials show hysteresis on thermal cycling, so calorimetric measurements were used to confirm the $T_{\rm C}$ variation. Powdered samples were thermally cycled between 0 and 180 °C in a Polymers Lab differential scanning calorimeter at a heating rate of 10 °C min⁻¹ and $T_{\rm C}$ values were extracted from the peak maximum associated with the endotherm in the cooling cycle. The two sets of $T_{\rm C}$ values are plotted *vs.* σ^2 in Fig. 2. A detailed analysis of the microstructure and electrical properties of the samples, which are sensitive to microstructural effects such as grain size and pellet density,⁹ will be reported elsewhere.

The two sets of $T_{\rm C}$ values both show a strong linear increase with increasing A-cation size variance, σ^2 , although the calorimetric values are systematically lower than those obtained from permittivity measurements. Linear fits to the permittivity and DSC results give slopes of $dT_C/d\sigma^2 = 14500(400)$ and 16000(300) K Å⁻², and $T_{\rm C}^{0}$ values (by extrapolation to $\sigma^2 = 0$) of 341(3) and 325(3) K, respectively, with fitting errors in parentheses. To estimate the contribution of cation size disorder to $T_{\rm C}$ in the Ba_{1-x}Ca_xCa_xTiO₃ series, the reported $T_{\rm C}$ values are shown together with disorder-corrected $T_{\rm C}^{0}$ values in Fig. 3. These were calculated in the first approximation by extrapolating from $T_{\rm C}$ to $\sigma^2 = 0$ assuming a constant $dT_{\rm C}/d\sigma^2 =$ 15 000 K Å⁻², although a slight variation in $dT_C/d\sigma^2$ is expected across the series by comparison with other systems.⁴ The resulting $T_{\rm C}^{0}$ values show a near-linear fall with x comparable to the behaviour of $T_{\rm C}$ in the Ba_{1-x}Sr_xTiO₃ series.²

These results show that the ferroelectric transition temperature in doped $BaTiO_3$ materials is strongly influenced by



Fig. 3 The variation of T_C (from ref. 3) and the disorder corrected T_C^0 in the $(Ba_{1-x}Ca_x)TiO_3$ series.

both the average A cation size $\langle r_A \rangle$ and the size variance σ^2 . These effects initially oppose one another in substituted $(Ba_{1-x}M_x)TiO_3$ series where Ba is replaced by smaller M = Sr or Ca cations. As x increases, the decreasing $\langle r_A \rangle$ reduces T_c but the increasing σ^2 raises T_C. The former reduction is essentially linear with $\langle r_A \rangle$, as evidenced by the T_C^0 variation in Fig. 3, in apparent contrast to the size dependence of the previously studied electronic transitions, which decrease quadratically with $\langle r_A \rangle$.^{4,6} The linear increase of T_C with σ^2 is in keeping with the observed variation of the structural transition in A_2CuO_4 materials. Reducing $\langle r_A \rangle$ in the ATiO₃ perovskites leads to tilts and rotations of the TiO₆ octahedra that destabilise the ferroelectrically ordered phase, whereas the local disorder associated with increasing σ^2 enables the ferroelectric distortions in the TiO₃ network to occur more easily and thereby stabilises the ferroelectric phase. This is supported by the data in Fig. 1, which show a divergence of the tetragonal a and cparameters as σ^2 increases.

The observed $dT_C/d\sigma^2 \approx 15000 \text{ K} \text{ Å}^{-2}$ in our ATiO₃ series is smaller than the value of $\approx 50000 \text{ K} \text{ Å}^{-2}$ found for the A₂CuO₄ structural transition,⁵ which involves rotations but not distortions of the CuO₆ octahedra. However, $dT_C/d\sigma^2$ is comparable to the reported magnitudes of $\approx 20000 \text{ K} \text{ Å}^{-2}$ for the metal–insulator transition in AMnO₃ perovskites.^{4,6} This is accompanied by the formation of Jahn–Teller distortions of the MnO₆ octahedra *above* the transition,¹⁰ whereas Ti displacements of comparable magnitude occur within the TiO₆ octahedra *below* the ferroelectric transition in ATiO₃ materials. Hence, the magnitude of $dT_C/d\sigma^2$ appears to be related to the degree of structural distortion occurring at the transition.

In conclusion, the ferroelectric–paraelectric transition temperature of ATiO₃ materials shows a strong linear increase with A-cation size variance. The σ^2 effect opposes the influence of the average A cation size and may be useful in stabilising ferroelectric phases to higher temperatures. In the $(Ba_{1-x}Sr_x)$ -TiO₃ series, the size effect dominates, so T_C falls with increasing x. However, Fig. 3 shows that the much greater σ^2 contribution in the $(Ba_{1-x}Ca_x)$ TiO₃ series effect; eading to almost constant T_C values up to the observed maximum x = 0.24.

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